## 

Post-quantum crypto on ARM Cortex-M

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## Crypto today

5 building blocks for a "secure channel" Symmetric crypto

- Block or stream cipher (e.g., AES, ChaCha20)
- Authenticator (e.g., HMAC, GMAC, Poly1305)
- Hash function (e.g., SHA-2, SHA-3)


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## Asymmetric crypto

- Key agreement / public-key encryption (e.g., RSA, Diffie-Hellman, ECDH)
- Signatures (e.g., RSA, DSA, ECDSA, EdDSA)


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The asymmetric monoculture

- All widely deployed asymmetric crypto relies on
- the hardness of factoring, or
- the hardness of (elliptic-curve) discrete logarithms


# Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer* 

Peter W. Shor ${ }^{\dagger}$


#### Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.


"In the past, people have said, maybe it's 50 years away, it's a dream, maybe it'll happen sometime. I used to think it was 50 . Now I'm thinking like it's 15 or a little more. It's within reach. It's within our lifetime. It's going to happen."
—Mark Ketchen (IBM), Feb. 2012, about quantum computers

## Post-quantum crypto

Definition
Post-quantum crypto is (asymmetric) crypto that resists attacks using classical and quantum computers.

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5 main directions

- Lattice-based crypto (PKE and Sigs)
- Code-based crypto (mainly PKE)
- Multivariate-based crypto (mainly Sigs)
- Hash-based signatures (only Sigs)
- Isogeny-based crypto (so far, mainly PKE)


## The NIST competition

| Count of Problem Category Column Labels $\mathrm{\nabla}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| Row Labels | v Key Exchange | Signature | Grand Total |
| ? | 1 |  | 1 |
| Braids | 1 | 1 | 2 |
| Chebychev | 1 |  | 1 |
| Codes | 19 | 5 | 24 |
| Finite Automata | 1 | 1 | 2 |
| Hash |  | 4 | 4 |
| Hypercomplex Numbers | 1 |  | 1 |
| Isogeny | 1 |  | 1 |
| Lattice | 24 | 4 | 28 |
| Mult. Var | 6 | 7 | 13 |
| Rand. walk | 1 |  | 1 |
| RSA | 1 | 1 | 2 |
| Grand Total | 57 | 23 | 80 |
| Q 4 | ¢て ${ }_{31} \quad \bigcirc_{27}$ | $\bullet$ |  |

Overview tweeted by Jacob Alperin-Sheriff on Dec 4, 2017.

## The NIST competition (ctd.)

"Key exchange"

- What is meant is key encapsulation mechanisms (KEMs)
- ( $\mathrm{vk}, \mathrm{sk}) \leftarrow$ KeyGen ()
- $(c, k) \leftarrow E n c a p s(v k)$
- $k \leftarrow \operatorname{Decaps}(c, s k)$
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Status of the NIST competition

- In total 69 submissions accepted as "complete and proper"
- Several broken, 5 withdrawn
- Jan 2019: NIST announces 26 round-2 candidates
- 17 KEMs and PKEs
- 9 signature schemes


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"... we will recommend that teams generally focus their hardware implementation efforts on Cortex-M4"
—Daniel Apon, Feb 2019

## pqm4

Joint work with
Matthias Kannwischer, Joost Rijneveld, and Ko Stoffelen.

- Started as part of PQCRYPTO H2O20 project
- Continued within EPOQUE ERC StG
- Library and testing/benchmarking framework
- PQ-crypto on ARM Cortex-M4
- Uses STM32F4 Discovery board
- 192 KB of RAM, benchmarks at 24 MHz
- Easy to add schemes using NIST API
- Optimized SHA3 and AES shared
 across primitives


## pqm4 usage

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- Run functional tests of all primitives and implementations:
python3 test.py
- Generate testvectors, compare for consistency (also with host): python3 testvectors.py
- Run speed and stack benchmarks:
python3 benchmarks.py
- Easy to evaluate only subset of schemes, e.g.:
python3 test.py newhope1024cca sphincs-shake256-128s


## Signatures (not) in pqm4

reference optimized
CRYSTALS-Dilithium FALCON
GeMSS
LUOV
MQDSS
Picnic
qTESLA
Rainbow
SPHINCS+

| $\checkmark$ | $(\checkmark)$ |
| :--- | :--- |
| $X_{\text {RAM }}$ | $\checkmark$ |
| $X_{\text {Key }}$ | - |
| $\checkmark$ | - |
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| $X_{\text {RAM }}$ | - |
| $\checkmark$ | - |
| $X_{\text {Key }}$ | - |
| $\checkmark$ | - |

$X_{\text {Key }}$ : keys too large $X_{\text {RAM }}$ : implementation uses too much RAM
$X_{\text {Lib }}$ : available implementations depend on external libraries

## KEMs (not) in pqm4



## Learning with errors (LWE)

- Given uniform $\mathbf{A} \in \mathbb{Z}_{q}^{k \times \ell}$
- Given "noise distribution" $\chi$
- Given samples As $+\mathbf{e}$, with $\mathbf{e} \leftarrow \chi$


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- Structured lattices: work in $\mathbb{Z}_{q}[x] / f$


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## Lattice-based KEMs - the basic idea

| Alice (server) |  | Bob (client) |
| :---: | :---: | :---: |
| $\mathbf{s , ~} \stackrel{L}{*}^{\text {s }} \chi$ |  | $\mathbf{s}^{\prime}, \mathbf{e}^{\prime} \stackrel{s}{5}^{5} \chi$ |
| $\mathbf{b} \leftarrow$ as $+\mathbf{e}$ | b | $\mathbf{u} \leftarrow \mathbf{a s}^{\prime}+\mathbf{e}^{\prime}$ |
|  | $u$ |  |

Alice has $\mathbf{v}=\mathbf{u s}=$ ass $^{\prime}+\mathbf{e}^{\prime} \mathbf{s}$
Bob has $\mathbf{v}^{\prime}=\mathbf{b s}^{\prime}=\mathbf{a s s}^{\prime}+\mathbf{e s}^{\prime}$

- Secret and noise $\mathbf{s}, \mathbf{s}^{\prime}, \mathbf{e}, \mathbf{e}^{\prime}$ are small
- $\mathbf{v}$ and $\mathbf{v}^{\prime}$ are approximately the same


## Core operation: multiplication in $\mathcal{R}_{q}=\mathbb{Z}_{q}[X] / f$

Power-of-two q

- Several schemes use $q=2^{m}$, for small $m$
- Examples: Round5, NTRU, Saber
- More round-1 examples: Kindi, RLizard


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## Prime "NTT-friendly" q

- Kyber and NewHope use prime q supporting fast NTT
- For $A, B \in \mathcal{R}_{q}, A \cdot B=\mathrm{NTT}^{-1}(\mathrm{NTT}(A) \circ \mathrm{NTT}(B))$
- NTT is Fourier Transform over finite field
- Use $f=X^{n}+1$ for power-of-two $n$


## Multiplication in $\mathbb{Z}_{2^{m}}[X]$

- Joint work with Matthias Kannwischer and Joost Rijneveld
- Represent coefficients as 16 -bit integers
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$$
\begin{aligned}
& \left(a_{\ell}+X^{k} a_{h}\right) \cdot\left(b_{\ell}+X^{k} b_{h}\right) \\
= & a_{\ell} b_{\ell}+X^{k}\left(a_{\ell} b_{h}+a_{h} b_{\ell}\right)+X^{n} a_{h} b_{h} \\
= & a_{\ell} b_{\ell}+X^{k}\left(\left(a_{\ell}+a_{h}\right)\left(b_{\ell}+b_{h}\right)-a_{\ell} b_{\ell}-a_{h} b_{h}\right)+X^{n} a_{h} b_{h}
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- Generalization: Toom-Cook
- Toom-3: split into 5 multiplications of $1 / 3$ size
- Toom-4: split into 7 multiplications of $1 / 4$ size
- Approach: Evaluate, multiply, interpolate


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- Optimize Saber, $q=2^{13}, n=256$
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- Is this the best approach? How about other values of $q$ and $n$ ?


## ©PTIMTHs



## Our approach

- Generate optimized assembly for Karatsuba/Toom
- Use Python scripts, receive as input $n$ and $q$
- Hand-optimize "small" schoolbook multiplications
- Make heavy use of DSP "vector instructions"
- Perform two $16 \times 16$-bit multiply-accumulate in one cycle
- Carefully schedule instructions to minimize loads/stores
- Benchmark different options, pick fastest


## Multiplication results

|  | approach | "small" | cycles | stack |
| :---: | :---: | :---: | :---: | :---: |
| Saber$\left(n=256, q=2^{13}\right)$ | Karatsuba only | 16 | 41121 | 2020 |
|  | Toom-3 | 11 | 41225 | 3480 |
|  | Toom-4 | 16 | 39124 | 3800 |
|  | Toom-4 + Toom-3 | - | - | - |
| Kindi-256-3-4-2$\left(n=256, q=2^{14}\right)$ | Karatsuba only | 16 | 41121 | 2020 |
|  | Toom-3 | 11 | 41225 | 3480 |
|  | Toom-4 | - | - | - |
|  | Toom-4 + Toom-3 | - | - | - |
| NTRU-HRSS$\left(n=701, q=2^{13}\right)$ | Karatsuba only | 11 | 230132 | 5676 |
|  | Toom-3 | 15 | 217436 | 9384 |
|  | Toom-4 | 11 | 182129 | 10596 |
|  | Toom-4 + Toom-3 | - | - | - |
| NTRU-KEM-743$\left(n=743, q=2^{11}\right)$ | Karatsuba only | 12 | 247489 | 6012 |
|  | Toom-3 | 16 | 219061 | 9920 |
|  | Toom-4 | 12 | 196940 | 11208 |
|  | Toom-4 + Toom-3 | 16 | 197227 | 12152 |
| $\begin{aligned} & \text { RLizard-1024 } \\ & (n=1024, \\ & \left.q=2^{11}\right) \end{aligned}$ | Karatsuba only | 16 | 400810 | 8188 |
|  | Toom-3 | 11 | 360589 | 13756 |
|  | Toom-4 | 16 | 313744 | 15344 |
|  | Toom-4 + Toom-3 | 11 | 315788 | 16816 |

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- Primary goal: optimize Kyber
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- Evaluate polynomial $f=f_{0}+f_{1} X+\cdots+f_{n-1} X^{n-1}$ at all $n$-th roots of unity
- Divide-and-conquer approach
- Write polynomial $f$ as $f_{0}\left(X^{2}\right)+X f_{1}\left(X^{2}\right)$
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\begin{aligned}
f(\beta) & =f_{0}\left(\beta^{2}\right)+\beta f_{1}\left(\beta^{2}\right) \text { and } \\
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- $f_{0}$ has $n / 2$ coefficients
- Evaluate $f_{0}$ at all ( $n / 2$ )-th roots of unity by recursive application
- Same for $f_{1}$


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- Pick up $f_{i}$ and $f_{i+2^{k}}$
- Multiply $f_{i+2^{k}}$ by a power of $\omega$ to obtain $t$
- Compute $f_{i+2^{k}} \leftarrow a_{i}-t$
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- Compute $f_{i+2^{k}} \leftarrow a_{i}-t$
- Compute $f_{i} \leftarrow a_{i}+t$
- Main optimizations on Cortex-M4:
- "Merge" levels: fewer loads/stores
- Optimize modular arithmetic (precompute powers of $\omega$ in Montgomery domain)
- Lazy reductions
- Carefully optimize using DSP instructions


## Selected optimized lattice KEM cycles

| Scheme | Key Generation | Encapsulation | Decapsulation |
| :--- | ---: | ---: | ---: |
| ntruhps2048509 | 77698713 | 645329 | 542439 |
| ntruhps2048677 | 144383491 | 955902 | 836959 |
| ntruhps4096821 | 211758452 | 1205662 | 1066879 |
| ntruhrss701 | 154676705 | 402784 | 890231 |
| lightsaber | 459965 | 651273 | 678810 |
| saber | 896035 | 1161849 | 1204633 |
| firesaber | 1448776 | 1786930 | 1853339 |
| kyber512 | 514291 | 652769 | 621245 |
| kyber768 | 976757 | 1146556 | 1094849 |
| kyber1024 | 1575052 | 1779848 | 1709348 |
| newhope1024cpa | 975736 | 975452 | 162660 |
| newhope1024cca | 1161112 | 1777918 | 1760470 |

Comparison: Curve25519 scalarmult: 625358 cycles

## Selected optimized lattice KEM stack bytes

| Scheme | Key Generation | Encapsulation | Decapsulation |
| :--- | ---: | ---: | ---: |
| ntruhps2048509 | 21412 | 15452 | 14828 |
| ntruhps2048677 | 28524 | 20604 | 19756 |
| ntruhps4096821 | 34532 | 24924 | 23980 |
| ntruhrss701 | 27580 | 19372 | 20580 |
| lightsaber | 9656 | 11392 | 12136 |
| saber | 13256 | 15544 | 16640 |
| firesaber | 20144 | 23008 | 24592 |
| kyber512 | 2952 | 2552 | 2560 |
| kyber768 | 3848 | 3128 | 3072 |
| kyber1024 | 4360 | 3584 | 3592 |
| newhope1024cpa | 11096 | 17288 | 8308 |
| newhope1024cca | 11080 | 17360 | 19576 |

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- Faster Keccak will accelerate several more schemes (e.g., Dilithium)
- NTRU-HPS is currently additionally bottlenecked by slow constant-time sorting
- Some more speedups possible ( $\approx 5 \%$ ?) by using floating-point registers
- NIST PQC website:
https://csrc.nist.gov/Projects/Post-Quantum-Cryptography
- NIST "PQC forum" mailing list:
https://csrc.nist.gov/projects/post-quantum-cryptography/ email-list
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- NIST "PQC forum" mailing list: https://csrc.nist.gov/projects/post-quantum-cryptography/ email-list
- pqm4 library and benchmarking suite: https://github.com/mupq/pqm4
- Code of $\mathbb{Z}_{2^{m}}[x]$ multiplication paper, including scripts: https://github.com/mupq/polymul-z2mx-m4
- $\mathbb{Z}_{2^{m}}[x]$ multiplication paper: https://cryptojedi.org/papers/\#latticem4
- Kyber/NTT optimization paper:
https://cryptojedi.org/papers/\#nttm4

