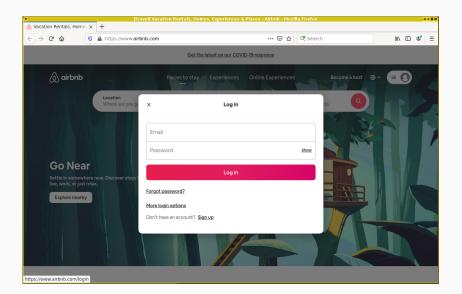
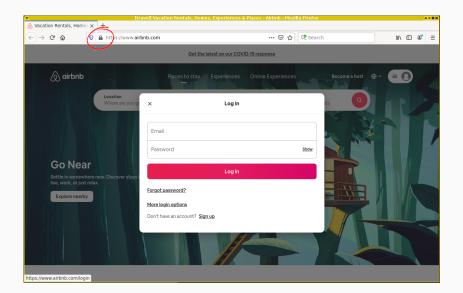


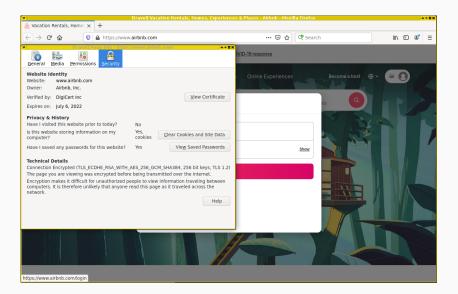


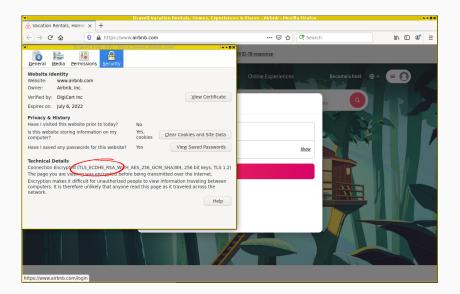
NIST PQC, Kyber, and beyond

August 10, 2022









Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer^{*}

Peter W. Shor[†]

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored. "In the past, people have said, maybe it's 50 years away, it's a dream, maybe it'll happen sometime. I used to think it was 50. Now I'm thinking like it's 15 or a little more. It's within reach. It's within our lifetime. It's going to happen."

-Mark Ketchen (IBM), Feb. 2012, about quantum computers

Definition

Post-quantum crypto is (asymmetric) crypto that resists attacks using classical *and quantum* computers.

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5 main directions

- Lattice-based crypto (PKE and Sigs)
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- Hash-based signatures (only Sigs)
- Isogeny-based crypto (so far, mainly PKE)

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- Selection through an open process and multiple rounds
- · Actual decisions are being made by NIST
- PQC project:
 - Announcement: Feb 2016
 - · Call for proposals: Dec 2016 (based on community input)
 - Deadline for submissions: Nov 2017

The NIST competition: initial overview

Count of Problem Catego	ry Column Labels 💌		
Row Labels	Key Exchange	Signature	Grand Total
?	1		1
Braids	1	1	2
Chebychev	1		1
Codes	19	5	24
Finite Automata	1	1	2
Hash		4	4
Hypercomplex Numbers	1		1
Isogeny	1		1
Lattice	24	4	28
Mult. Var	6	7	13
Rand. walk	1		1
RSA	1	1	2
Grand Total	57	23	80
Q 4	1] 31 ♥ 27		

Overview tweeted by Jacob Alperin-Sheriff on Dec 4, 2017.

Announcement planned at Real-World Crypto 2019

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Signature schemes

- 3 lattice-based
- 2 symmetric-crypto based
- 4 MQ-based

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- 4 key-agreement schemes
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Finalists

- 4 key-agreement schemes
 - · 3 lattice-based
 - 1 code-based
- 3 signature schemes
 - 2 lattice-based
 - 1 MQ-based

Alternate schemes

- 5 key-agreement schemes
 - · 2 lattice-based
 - 2 code-based
 - 1 isogeny-based
- 3 signature schemes
 - 2 symmetric-crypto based
 - 1 MQ-based

Announcement planned for March 2022

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 - CRYSTALS-Kyber: lattice-based key agreement
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 - Falcon: lattice-based signature
 - SPHINCS⁺: hash-based signature

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4 schemes advanced to round 4

- Classic McEliece: code-based key agreement
- BIKE: code-based key agreement
- HQC: code-based key agreement
- SIKE: isogeny-based key agreement

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4 schemes advanced to round 4

- Classic McEliece: code-based key agreement
- BIKE: code-based key agreement
- HQC: code-based key agreement
- SIKE: isogeny-based key agreement
- Additionally: call for more signature proposals

What now?

- Standards ready "by 2024"
- Time to start upgrading systems!

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Store now, decrypt later



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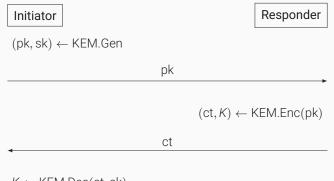


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Let's understand Kyber and what it means to use it.

A long time ago (2015) in a galaxy far, far away (Šibenik, Croatia)....

What is a Key Encapsulation Mechanism (KEM)?



 $K \leftarrow \mathsf{KEM}.\mathsf{Dec}(\mathsf{ct},\mathsf{sk})$

- Given \mathbf{a} , uniformly random
- Given "noise distribution" χ
- Given samples $\mathbf{as} + \mathbf{e}$, with $\mathbf{e} \leftarrow \chi$

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- Given "noise distribution" χ
- Given samples $\mathbf{as} + \mathbf{e}$, with $\mathbf{e} \leftarrow \chi$
- Search version: find ${\bf s}$
- Decision version: distinguish from uniform random

Short answer In $\mathcal{R}_q = \mathbb{Z}_q[X]/(X^n + 1)$

Longer answer

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

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Example

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

$$\mathbf{a} + \mathbf{b} = 10X^3 + 9X^2 + 2X + 5$$

= $3X^3 + 2X^2 + 2X + 5$

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

$$\mathbf{a} - \mathbf{b} = -2X^3 + X^2 + 2X - 1$$

= 5X³ + X² + 2X + 6

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

Example

$$\mathbf{a} \cdot \mathbf{b} = 24X^6 + 16X^5 + 12X^3 + 30X^5 + 20X^4 + 15X^2 + 12X^4 + 8X^3 + 6X + 12X^3 + 8X^2 + 6$$

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

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$$= 24X^{6} + 46X^{5} + 32X^{4} + 32X^{3} + 23X^{2} + 6$$

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= 24X⁶ + 46X⁵ + 32X⁴ + 32X³ + 23X² + 6
= 3X⁶ + 4X⁵ + 4X⁴ + 4X³ + 2X² + 6
= -3X² - 4X - 4 + 4X³ + 2X² + 6

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

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= $-X^{2} - 4X + 4X^{3} + 2$

Polynomials with *n* coefficients, each coefficient in $\{0, ..., q-1\}$ Arithmetic uses reduction modulo *q* and modulo $(X^n + 1)$

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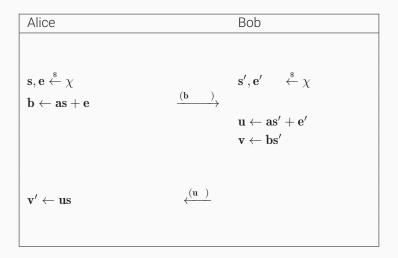
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$$= -X^{2} - 4X + 4X^{3} + 2$$

$$= 4X^{3} + 6X^{2} + 3X + 2$$

Alice (server)		Bob (client)
$\mathbf{s}, \mathbf{e} \xleftarrow{\hspace{0.1cm}} \chi$		$\mathbf{s}', \mathbf{e}' \xleftarrow{\hspace{0.15cm} \$} \chi$
$\mathbf{b} \leftarrow \mathbf{as} + \mathbf{e}$	$\xrightarrow{ \ \ b \ \ }$	$\mathbf{u} \gets \mathbf{a}\mathbf{s}' + \mathbf{e}'$
	\xleftarrow{u}	

- Secret and noise polynomials $\mathbf{s},\mathbf{s}',\mathbf{e},\mathbf{e}'$ are small
- \mathbf{v} and \mathbf{v}' are approximately the same



Alice		Bob
seed $\stackrel{\hspace{0.1em}\scriptscriptstyle\$}{\leftarrow} \{0,1\}^{256}$		
$\mathbf{a} \leftarrow Parse(XOF(\mathit{seed}))$		
$\mathbf{s}, \mathbf{e} \xleftarrow{\hspace{0.1cm}\$} \chi$		$\mathbf{s}', \mathbf{e}' \qquad \stackrel{\$}{\leftarrow} \chi$
$\mathbf{b} \leftarrow \mathbf{as} + \mathbf{e}$	$\xrightarrow{(\mathbf{b}, \textit{seed})}$	$\mathbf{a} \leftarrow Parse(XOF(\textit{seed}))$
		$\mathbf{u} \leftarrow \mathbf{a}\mathbf{s}' + \mathbf{e}'$
		$\mathbf{v} \leftarrow \mathbf{b} \mathbf{s}'$
	<i>.</i>	
$\mathbf{v}' \leftarrow \mathbf{us}$	$\stackrel{(\mathbf{u})}{\longleftarrow}$	

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		$\mathbf{v} \leftarrow \mathbf{b} \mathbf{s}'$
		$k \stackrel{\hspace{0.1em}\scriptscriptstyle\$}{\leftarrow} \{0,1\}^n$
		$\mathbf{k} \leftarrow Encode(k)$
$\mathbf{v}' \leftarrow \mathbf{us}$	$\xleftarrow{(\mathbf{u},\mathbf{c})}$	$\mathbf{c} \gets \mathbf{v} + \mathbf{k}$

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$\mathbf{k}' \leftarrow \mathbf{c} - \mathbf{v}'$		$\mu \gets Extract(\mathbf{k})$
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This is LPR encryption, written as KEM (except for generation of \mathbf{a})

- Encoding in LPR encryption: map *n* bits to *n* coefficients:
 - A zero bit maps to 0
 - A one bit maps to q/2
- · Idea: Noise affects low bits of coefficients, put data into high bits

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 - A zero bit maps to 0
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- · Idea: Noise affects low bits of coefficients, put data into high bits
- Decode: map coefficient into [-q/2, q/2]
 - Closer to 0 (i.e., in $\left[-q/4, q/4\right]$): set bit to zero
 - Closer to $\pm q/2$: set bit to one



Roberto Avanzi Léo Ducas Vadim Lyubashevsky John M. Schanck Peter Schwabe Gregor Seiler

Joppe Bos Eike Kiltz Damien Stehlé Jintai Ding Tancrede Lepoint

MLWE instead of RLWE

IND-CCA2 Security

MLWE instead of RLWE

- Easily scale security
- Optimized routines the same for all security levels

IND-CCA2 Security

MLWE instead of RLWE

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- Optimized routines the same for all security levels

IND-CCA2 Security

- Support static (or cached) keys
- More robust
- Useful for authenticated key exchange
- Easy to construct PKE

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- For example, NEWHOPE uses n = 1024, q = 12289
- MLWE uses matrices and vectors of smaller polynomials of small dimension
- Kyber: *n* = 256, *q* = 3329
 - Security level 1 (AES-128): d = 2
 - Security level 3 (AES-192): *d* = 3
 - Security level 5 (AES-256): d = 4
- Core arithmetic is in $\mathbb{Z}_{3329}[X]/(X^{256}+1)$ for all security levels

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 - Security level 5 (AES-256): d = 4
- Core arithmetic is in $\mathbb{Z}_{3329}[X]/(X^{256}+1)$ for all security levels
- Noise is centered binomial HW(x) HW(y) for 2-bit x and y

Chosen-ciphertext attacks

- Decryption failures are a function of $\mathbf{s}, \mathbf{e}, \mathbf{s}', \mathbf{e}'$
- Attacker can choose larger secret/noise \mathbf{e}' and \mathbf{s}'
- Observe if decryption fails
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- Observe if decryption fails
- Learn something about ${\bf s}$
- This is a chosen ciphertext attack (CCA)
- Learn full ${\bf s}$ after a few thousand queries
- NEWHOPE never claimed CCA-security!
- This "attack" is completely expected
- Not a problem for ephemeral ${\bf s}$

The Fujisaki-Okamoto Transform (idea)

- Build CCA-secure KEM from passively secure encryption scheme
- Make failure probability negligible for honest $\mathbf{s}', \mathbf{e}', \mathbf{e}''$
- Force encapsulator to generate $\mathbf{s}^\prime,\,\mathbf{e}^\prime,\,\mathbf{e}^{\prime\prime}$ honestly

From passive to CCA security

The Fujisaki-Okamoto Transform

Alice (Server)		Bob (Client)
<u>Gen()</u> :	nk	Encaps(pk):
$pk,sk \leftarrow KeyGen()$	$\xrightarrow{\rho\kappa}$	$\begin{array}{l} x \leftarrow \{0, \dots, 255\}^{32} \\ k, \text{coins} \leftarrow \text{SHA3-512}(x) \end{array}$
	€t	$ct \leftarrow Encrypt(pk, x, coins)$
Decaps((sk, pk), ct):		
$x' \leftarrow \text{Decrypt(sk, ct)}$		
$k', coins' \leftarrow SHA3-512(x')$		
$ct' \leftarrow Encrypt(pk, x', coins')$ verify if $ct = ct'$		

From passive to CCA security

The Fujisaki-Okamoto Transform

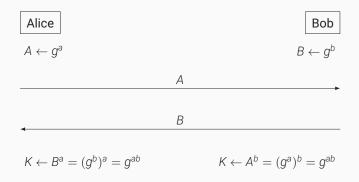
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Gen():		Encaps(pk):
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$\begin{array}{l} \underline{Decaps}((sk,pk),ct):\\ \overline{x'}\leftarrow Decrypt(sk,ct)\\ k',\mathit{coins'}\leftarrowSHA3-512(x')\\ ct'\leftarrowEncrypt(pk,x',\mathit{coins'})\\ \mathbf{verify}\ \mathbf{if}\ ct=ct' \end{array}$	¢t ←	$ct \leftarrow Encrypt(pk, x, coins)$

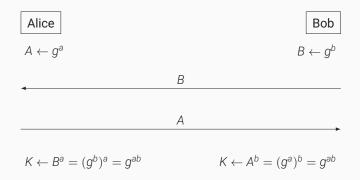
Additionally in Kyber:

- Hash the (hash of the) public key into x
 - Multi-target protection (for coins)
 - Turn into contributory KEM
- Hash the (hash of the) ciphertext into the final key

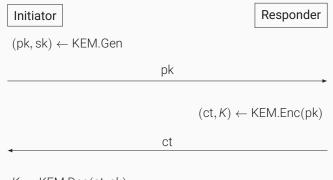
Key exchange today: ECDH

- Key-pair generation $\approx 125,000$ Comet Lake cycles
- Shared-key computation $\approx 125,000$ Comet Lake cycles
- Public keys have 32 bytes





Kyber for Engineers, part I: A KEM is not DH!



 $K \leftarrow \mathsf{KEM}.\mathsf{Dec}(\mathsf{ct},\mathsf{sk})$

Kyber768 (NIST Security level 3)

- Key-pair generation $\approx 40,000$ Comet Lake cycles
- Encapsulation $\approx 55,000$ Comet Lake cycles
- Decapsulation $\approx 45,000$ Comet Lake cycles

Kyber768 (NIST Security level 3)

- Key-pair generation $\approx 40,000$ Comet Lake cycles
- Encapsulation $\approx 55,000$ Comet Lake cycles
- Decapsulation $\approx 45,000$ Comet Lake cycles
- Public keys have 1184 bytes
- Ciphertexts have 1088 bytes

Kyber768 (NIST Security level 3)

- Key-pair generation $\approx 40,000$ Comet Lake cycles
- Encapsulation $\approx 55,000$ Comet Lake cycles
- Decapsulation $\approx 45,000$ Comet Lake cycles
- Public keys have 1184 bytes
- · Ciphertexts have 1088 bytes
- Cycles are dominated by Keccak!

Kyber for Engineers, part III: SCA and FI against FO

- FO-transform: hide if decryption succeeded
- Use full re-encryption to do this

- FO-transform: hide if decryption succeeded
- Use full re-encryption to do this
- Long computation, one bit of information
- Very hard to protect against SCA/FI

- Start playing with Kyber
- Assume that details may still change

- Start playing with Kyber
- · Assume that details may still change
- Always combine with pre-quantum crypto (hybrid KEMs)
- Use Kyber768 (or Kyber1024)

- Will need to migrate to PQC in the next 5-10 years
- Use this to migrate to high-assurance implementations!
 - Computer-verified correctness
 - Computer-verified security
 - · Computer-verified implementation security

https://formosa-crypto.org

Online references

• NIST PQC website:

https://csrc.nist.gov/Projects/Post-Quantum-Cryptography

- NIST mailing list: https://csrc.nist.gov/projects/post-quantum-cryptography/ email-list https://groups.google.com/a/list.nist.gov/g/pqc-forum
- Kyber:

https://pq-crystals.org/kyber https://github.com/pq-crystals/kyber