

Post-quantum crypto on ARM Cortex-M

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PQCRYPTO

- Project funded by EU in Horizon 2020.
- Running from March 2015 until February 2018
- 11 partners from academia and industry, TU/e was coordinator
- 22 submissions to NIST PQC project



- Find post-quantum secure cryptosystems suitable for small devices in power and memory requirements (e.g. smart cards with 8-bit or 16-bit or 32-bit architectures, with different amounts of RAM)
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 - SPHINCS⁺: 8–50 KB signatures
- Additional challenges:
 - Computational complexity
 - Implementation security



- ARM Cortex-M4 on STM32F4-Discovery board
- 192KB RAM, 1MB Flash (ROM)
- Available for <20 Euros from various vendors (e.g., Amazon, RS Components, Conrad)



Joint work with

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- Library and testing/benchmarking framework
- Easy to add schemes using NIST API
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- Easy to add schemes using NIST API
- Optimized SHA3 shared across primitives
- Run functional tests of all primitives and implementations: python3 test.py
- Generate testvectors, compare for consistency (also with host): python3 testvectors.py
- Run speed and stack benchmarks: python3 benchmarks.py
- Easy to evaluate only subset of schemes, e.g.: python3 test.py newhope1024cca sphincs-shake256-128s

BIG QUAKE BIKE Classic McEliece **CRYSTALS-Kyber** DAGS FrodoKEM KINDI NewHope NTRU-HRSS-KEM **NTRU** Prime Post-quantum RSA-Encryption Ramstake SABER SIKE

X

X

X(?)



CRYSTALS-Dilithium GUI LUOV MQDSS Picnic Post-quantum RSA-Signature qTESLA Rainbow SPHINCS+

✓ × ? ×(?) × × ✓ ? (probably no) ✓



From PQCRYPTO to EPOQUE

- Since October 2018 working on ERC project Engineering post-quantum cryptography – EPOQUE
- WP1: Secure implementations of post-quantum crypto
- Build on results of PQCRYPTO, e.g., extend pqm4:
 - Include more optimized implementations
 - Include implementations with SCA protection

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- First paper of EPOQUE:

Matthias Kannwischer, Joost Rijneveld, Peter Schwabe. *Faster* multiplication in $\mathbb{Z}_{2^m}[x]$ on Cortex-M4 to speed up NIST PQC candidates.

• Speed up 5 lattice-based KEMs

- Given uniform $\mathbf{A} \in \mathbb{Z}_q^{k imes \ell}$
- $\bullet\,$ Given "noise distribution" χ
- Given samples $\mathbf{As} + \mathbf{e}$, with $\mathbf{e} \leftarrow \chi$



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Alice (server)		Bob (client)
$\mathbf{s}, \mathbf{e} \xleftarrow{\hspace{0.15cm}} \chi$		$\mathbf{s'}, \mathbf{e'} \xleftarrow{\hspace{0.15cm} \$} \chi$
$\mathbf{b} \leftarrow \mathbf{as} + \mathbf{e}$	$\xrightarrow{ \ \ b} \\ \longrightarrow$	$\mathbf{u}{\leftarrow}\mathbf{a}\mathbf{s}'+\mathbf{e}'$
	←	

Alice has $\mathbf{v} = \mathbf{us} = \mathbf{ass'} + \mathbf{e's}$ Bob has $\mathbf{v'} = \mathbf{bs'} = \mathbf{ass'} + \mathbf{es'}$

- Secret and noise $\boldsymbol{s}, \boldsymbol{s}', \boldsymbol{e}, \boldsymbol{e}'$ are small
- t and t' are approximately the same

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- Why optimize those 5 KEMs?
 - Have to start somewhere...
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- How to optimize those 5 KEMs?
 - Faster multiplication of polynomials with n coefficients over $\mathbb{Z}_{2^m}[x]$

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- Can do better using Karatsuba:

$$\begin{aligned} &(a_{\ell} + X^{k}a_{h}) \cdot (b_{\ell} + X^{k}b_{h}) \\ &= a_{\ell}b_{\ell} + X^{k}(a_{\ell}b_{h} + a_{h}b_{\ell}) + X^{n}a_{h}b_{h} \\ &= a_{\ell}b_{\ell} + X^{k}((a_{\ell} + a_{h})(b_{\ell} + b_{h}) - a_{\ell}b_{\ell} - a_{h}b_{h}) + X^{n}a_{h}b_{h} \end{aligned}$$

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- Generalization: Toom-Cook
 - Toom-3: split into 5 multiplications of 1/3 size
 - Toom-4: split into 7 multiplications of 1/4 size
- Approach: Evaluate, multiply, interpolate

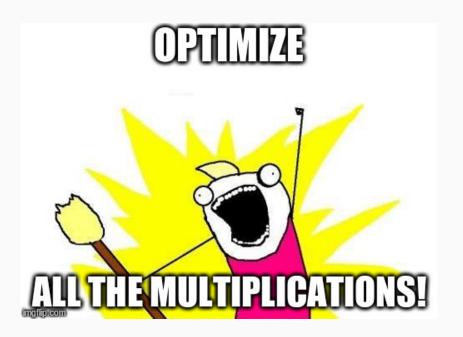
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 - Optimize Saber, $q = 2^{13}, n = 256$
 - Use Toom-4 + two levels of Karatsuba
 - Optimized 16-coefficient schoolbook multiplication

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- Is this the best approach? How about other values of q and n?



- Generate optimized assembly for Karatsuba/Toom
- Use Python scripts, receive as input n and q
- Hand-optimize "small" schoolbook multiplications
- Benchmark different options, pick fastest



Fast schoolbook multiplication

- ARMv7E-M supports SMUAD(X) and SMLAD(X)
- All in one clock cycle
- Perfect for polynomial multiplication

instruction	semantics
smuad Ra, Rb, Rc	$\mathtt{Ra} \leftarrow \mathtt{Rb}_\mathtt{L} \cdot \mathtt{Rc}_\mathtt{L} + \mathtt{Rb}_\mathtt{H} \cdot \mathtt{Rc}_\mathtt{H}$
smuadx Ra, Rb, Rc	$\mathtt{Ra} \leftarrow \mathtt{Rb}_\mathtt{L} \cdot \mathtt{Rc}_\mathtt{H} + \mathtt{Rb}_\mathtt{H} \cdot \mathtt{Rc}_\mathtt{L}$
smlad Ra, Rb, Rc, Rd	$\mathtt{Ra} \leftarrow \mathtt{Rb}_\mathtt{L} \cdot \mathtt{Rc}_\mathtt{L} + \mathtt{Rb}_\mathtt{H} \cdot \mathtt{Rc}_\mathtt{H} + \mathtt{Rd}$
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Fast schoolbook multiplication [N=2]



Fast schoolbook multiplication [N=2]

 a_5b_3 a_4b_3 a_3b_3 a_2b_3 a_1b_3 a_0b_3

 a_5b_5 a_4b_5 a_3b_5 a_2b_5 a_1b_5 a_0b_5

• 3 multiplications instead of 4

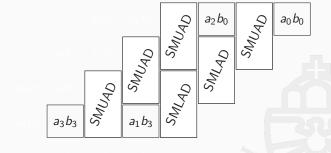
Fast schoolbook multiplication [N=4]

			a ₃ b ₀	a_2b_0	a_1b_0	$a_0 b_0$	
		a_3b_1	a_2b_1	a_1b_1	a_0b_1		
	a_3b_2	a_2b_2	a_1b_2	$a_0 b_2$			
<i>a</i> ₃ <i>b</i> ₃	<i>a</i> ₂ <i>b</i> ₃	a_1b_3	a_0b_3				

 a_5b_4 a_4b_4 a_3b_4 a_2b_4 a_1b_4 a_0

 a_5b_5 a_4b_5 a_3b_5 a_2b_5 a_1b_5 a_0b_5

Fast schoolbook multiplication [N=4]

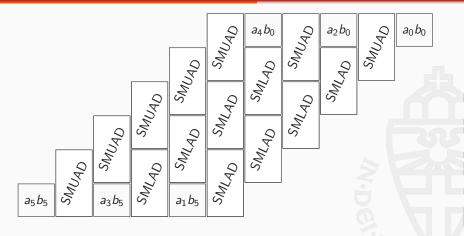


• 10 multiplications instead of 16

Fast schoolbook multiplication [N=6]

					$a_5 b_0$	a4 b0	a_3b_0	a_2b_0	a_1b_0	$a_0 b_0$	
				a_5b_1	a_4b_1	a_3b_1	a_2b_1	a_1b_1	a_0b_1		
			a_5b_2	a_4b_2	a_3b_2	a_2b_2	a_1b_2	a_0b_2			
		a_5b_3	a_4b_3	a ₃ b ₃	a2b3	a_1b_3	a_0b_3				
	a_5b_4	a4 b4	a3b4	a ₂ b ₄	a_1b_4	a ₀ b ₄					
a_5b_5	a_4b_5	a3b5	a_2b_5	a_1b_5	$a_0 b_5$						

Fast schoolbook multiplication [N=6]



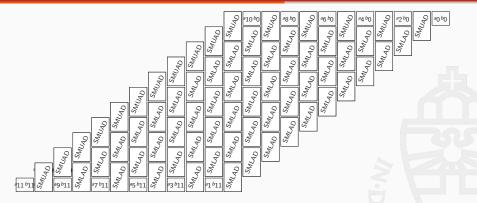
• 21 multiplications instead of 36

Fast schoolbook multiplication [N=12]

						^ə 11 ^b 0	^a 10 ^b 0	^{ag b} 0	^a 8 ^b 0	^a 7 ^b 0	^a 6 ^b 0	a5 b0	^a 4 ^b 0	^a 3 <i>b</i> 0	^a 2 ^b 0	^a 1 ^b 0	^a 0 ^b 0
					^a 11 ^b 1	^ə 10 ^b 1	^a 9 ^b 1	^a 8 ^b 1	^a 7 ^b 1	^a 6 ^b 1	^a 5 ^b 1	^a 4 ^b 1	^a 3 ^b 1	^a 2 ^b 1	^a 1 ^b 1	^a 0 ^b 1	
				^a 11 ^b 2	^a 10 ^b 2	^a 9 ^b 2	^a 8 ^b 2	^a 7 ^b 2	^a 6 ^b 2	^a 5 ^b 2	^a 4 ^b 2	^a 3 ^b 2	^a 2 ^b 2	^a 1 ^b 2	^a 0 ^b 2		
		a	11 ^b 3	^a 10 ^b 3	^a 9 ^b 3	^{38 b} 3	^a 7 ^b 3	^a 6 ^b 3	^a 5 ^b 3	^a 4 ^b 3	^a 3 ^b 3	^a 2 ^b 3	^a 1 ^b 3	^a 0 ^b 3			
		^a 11 ^b 4 ^a	10 ^b 4	^a 9 ^b 4	^a 8 ^b 4	^a 7 ^b 4	^a 6 ^b 4	^a 5 ^b 4	^a 4 ^b 4	^a 3 ^b 4	^a 2 ^b 4	^a 1 ^b 4	^a 0 ^b 4				
	² 11 ^b 5	^a 10 ^b 5	^a 9 ^b 5	^a 8 ^b 5	^a 7 ^b 5	^a 6 ^b 5	^a 5 ^b 5	^a 4 ^b 5	^a 3 ^b 5	^a 2 ^b 5	^a 1 ^b 5	^a 0 ^b 5					
a	11 ^b 6 ^a 10 ^b 6	^a 9 ^b 6	^a 8 ^b 6	^a 7 ^b 6	^a 6 ^b 6	^a 5 ^b 6	^a 4 ^b 6	^a 3 ^b 6	^a 2 ^b 6	^a 1 ^b 6	^a 0 ^b 6						
³ 11 ^b 7	10 b7 39 b7	38 b7	^a 7 ^b 7	^a 6 ^b 7	^a 5 ^b 7	^a 4 ^b 7	^a 3 <i>b</i> 7	^a 2 ^b 7	^a 1 ^b 7	^a 0 ^b 7							
² 11 ^b 8 ² 10 ^b 8	ag bg ag bg	^a 7 ^b 8	^a 6 ^b 8	^a 5 ^b 8	^a 4 ^b 8	^a 3 ^b 8	^a 2 ^b 8	^a 1 ^b 8	^a 0 ^b 8								
² 11 ^b 9 ² 10 ^b 9 ² 9 ^b 9	^a 8 b9 a7 b9	^a 6 ^b 9	^a 5 ^b 9	^a 4 ^b 9	^a 3 <i>b</i> 9	^a 2 ^b 9	^a 1 ^b 9	^a 0 ^b 9									
² 11 ^b 10 ¹ 10 ^b 10 ² 9 ^b 10 ² 8 ^b 10 ²	7 ^b 10 ^a 6 ^b 10	^a 5 ^b 10 ^a	4 <i>^b</i> 10	^a 3 ^b 10	^a 2 ^b 10	^ə 1 ^b 10	^a 0 ^b 10										
² 11 ^b 11 ² 10 ^b 11 ² 9 ^b 11 ² 8 ^b 11 ² 7 ^b 11 ²	6 ^b 11 ^b 5 ^b 11	^a 4 ^b 11 ^a	3 <i>b</i> 11	^a 2 ^b 11	³ 1 ^b 11	^a 0 ^b 11											

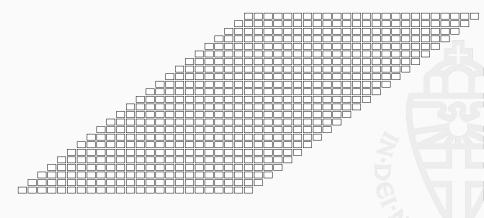
- How many can we fit in registers?
- 16 registers minus SP and PC \rightarrow we fit 24 coefficients

Fast schoolbook multiplication [N=12]

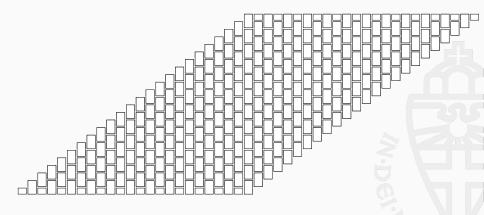


- How many can we fit in registers?
- + 16 registers minus SP and PC \rightarrow we fit 24 coefficients
- 78 multiplications instead of 144

Fast schoolbook multiplication [N=24]

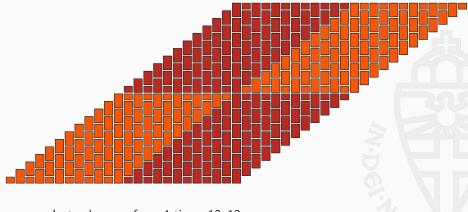


Fast schoolbook multiplication [N=24]



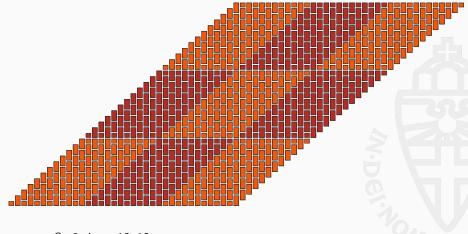
• We want to merge all, but not enough registers

Fast schoolbook multiplication [N=24]



• Instead we perform 4 times 12×12

Fast schoolbook multiplication [N=36]



• Or 9 times 12x12

					a_5b_0	a4 b0	a ₃ b ₀	a_2b_0	a_1b_0	a ₀ b ₀	
				a_5b_1	a_4b_1	a_3b_1	a_2b_1	a_1b_1	a_0b_1		
			a_5b_2	a4b2	a ₃ b ₂	a ₂ b ₂	a ₁ b ₂	$a_0 b_2$			
		a_5b_3	a ₄ b ₃	a3b3	a2b3	a_1b_3	a_0b_3				
	a_5b_4	a4 b4	a ₃ b ₄	a ₂ b ₄	a_1b_4	a ₀ b ₄					
$a_5 b_5$	a_4b_5	a_3b_5	a_2b_5	a_1b_5	a_0b_5						

- $R3 = b_1 | b_0, R4 = b_3 | b_2, R5 = b_5 | b_4$

					a_5b_0	a4 b0	a_3b_0	a_2b_0	a_1b_0	$a_0 b_0$	
				a_5b_1	a_4b_1	a_3b_1	a_2b_1	a_1b_1	a_0b_1		
			a_5b_2	a ₄ b ₂	a ₃ b ₂	a2b2	a_1b_2	a_0b_2			
		a ₅ b ₃	a4b3	a3b3	a2b3	a_1b_3	a ₀ b ₃				
	a_5b_4	a4b4	a ₃ b ₄	a2b4	a_1b_4	a ₀ b ₄					
$a_5 b_5$	a_4b_5	a3 b5	a_2b_5	a_1b_5	a_0b_5						

- $R0 = a_1 | a_0, R1 = a_3 | a_2, R2 = a_5 | a_4$
- $R3 = b_1 | b_0, R4 = b_3 | b_2, R5 = b_5 | b_4$
- For even columns we need to repack b

					a_5b_0	$a_4 b_0$	a ₃ b ₀	$a_2 b_0$	a_1b_0	$a_0 b_0$	
				a_5b_1	a_4b_1	a_3b_1	a_2b_1	a_1b_1	a_0b_1		
			a_5b_2	a_4b_2	a3b2	a_2b_2	a_1b_2	$a_0 b_2$			
		$a_5 b_3$	a4b3	a ₃ b ₃	a2b3	a_1b_3	a ₀ b ₃				
	$a_5 b_4$	$a_4 b_4$	a3b4	a_2b_4	a_1b_4	$a_0 b_4$					
$a_5 b_5$	a_4b_5	$a_{3}b_{5}$	a_2b_5	a_1b_5	a ₀ b ₅						

- $R0 = a_1 | a_0, R1 = a_3 | a_2, R2 = a_5 | a_4$
- $R3 = b_1|b_0, R4 = b_3|b_2, R5 = b_5|b_4$
- First do odd columns

					$a_5 b_0$	a ₄ b ₀	a3 b0	a_2b_0	a_1b_0	$a_0 b_0$	
				a_5b_1	a_4b_1	a_3b_1	a_2b_1	a_1b_1	$a_0 b_1$		
			a_5b_2	a4b2	a_3b_2	a2b2	a_1b_2	$a_0 b_2$			
		a_5b_3	a_4b_3	a3b3	a_2b_3	a_1b_3	$a_0 b_3$		-		
	$a_5 b_4$	a4 b4	a_3b_4	a2b4	a_1b_4	a ₀ b ₄					
$a_{5}b_{5}$	a_4b_5	a3 b5	a_2b_5	a ₁ b ₅	$a_0 b_5$						

- $R0 = a_1 | a_0, R1 = a_3 | a_2, R2 = a_5 | a_4$
- Then repack to $R3 = b_2|b_1, R4 = b_4|b_3$ and do even columns

Multiplication results

	approach	"small"	cycles	stack
	Karatsuba only	16	41 121	2 0 2 0
Saber	Toom-3	11	41 225	3 480
$(n = 256, q = 2^{13})$	Toom-4	16	39 124	3 800
	Toom-4 + Toom-3	-	-	-
	Karatsuba only	16	41 121	2 0 2 0
Kindi-256-3-4-2	Toom-3	11	41 225	3 480
$(n = 256, q = 2^{14})$	Toom-4	-	-	_
	Toom-4 + Toom-3	-	-	
	Karatsuba only	11	230 132	5 676
NTRU-HRSS	Toom-3	15	217 436	9 384
$(n = 701, q = 2^{13})$	Toom-4	11	182 129	10 596
	Toom-4 + Toom-3	-		
	Karatsuba only	12	247 489	6 0 1 2
NTRU-KEM-743	Toom-3	16	219 061	9 9 2 0
$(n = 743, q = 2^{11})$	Toom-4	12	196 940	11 208
	Toom-4 + Toom-3	16	197 227	12 152
RLizard-1024	Karatsuba only	16	400 810	8 1 8 8
	Toom-3	11	360 589	13756
$(n = 1024, \dots, 211)$	Toom-4	16	313744	15 344
$q = 2^{11}$)	Toom-4 + Toom-3	11	315 788	16816

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- \bullet Between 69% and 92% of cycles spent in mul+hash

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NISTPQC code quality...

- Fix misunderstandings of NIST API
- Remove all dynamic memory allocations
- Fix some obvious timing leakages
- More work required, for many NIST submissions!

	implementation	clo	ck cycles	stac	k usage
		K:	6 530 <i>k</i>	K:	12616
	Reference	E:	8 684 <i>k</i>	E:	14896
		D:	10 581 <i>k</i>	D:	15 992
		K:	1147 <i>k</i>	K:	13883
Saber	[KBSV18]	E:	1444 <i>k</i>	E:	16667
		D:	1 543 <i>k</i>	D:	17763
		K:	949 <i>k</i>	K:	13248
	This work	E:	1 232 <i>k</i>	E:	15 528
		D:	1 260 <i>k</i>	D:	16624
		K:	21794 <i>k</i>	K:	59864
	Reference	E:	28 176 <i>k</i>	E:	71000
Kindi-256-3-4-2		D:	37 129 <i>k</i>	D:	84 096
KIIIui-230-3-4-2		K:	1010 <i>k</i>	K:	44 264
	This work	E:	1 365 <i>k</i>	E:	55 392
		D:	1 563 <i>k</i>	D:	64 376

KEM results

	implementation	clo	ck cycles	stac	k usage
		K:	205 156 <i>k</i>	K:	10 0 20
	Reference	E:	5 166 <i>k</i>	E:	8 956
NTRU-HRSS		D:	15 067 <i>k</i>	D:	10 204
NTRO-HR33		K:	161 790 <i>k</i>	K:	23 396
	This work	E:	432 <i>k</i>	E:	19 492
		D:	863 <i>k</i>	D:	22140
		K:	59 815 <i>k</i>	K:	14 148
	Reference	E:	7 540 <i>k</i>	E:	13 372
NTRU-KEM-743		D:	14 229 <i>k</i>	D:	18036
NTRO-REIVI-743		K:	5 663 <i>k</i>	K:	25 320
	This work	E:	1 655 <i>k</i>	E:	23 808
		D:	1 904 <i>k</i>	D:	28 472
		K:	26 423 <i>k</i>	K:	4 272
	Reference	E:	32 156 <i>k</i>	E:	10532
RLizard-1024		D:	53 181 <i>k</i>	D:	12 6 3 6
NLIZaru-1024		K:	537 <i>k</i>	K:	27720
	This work	E:	1 358 <i>k</i>	E:	33 328
		D:	1 740 <i>k</i>	D:	35 448

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- Idea: collect "clean" implementations once

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- At the moment still setting up CI
- Hope to be done soon, then PRs very welcome!

The definition of "clean"

- Code is valid C99
- Passes functional tests
- API functions do not write outside provided buffers
- Compiles with -Wall -Wextra -Wpedantic -Werror with gcc and clang
- Consistent test vectors across runs
- Consistent test vectors on big-endian and little-endian machines
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- Consistent test vectors across runs
- Consistent test vectors on big-endian and little-endian machines
- Consistent test vectors on 32-bit and 64-bit machines
- No errors/warnings reported by valgrind
- No errors/warnings reported by address sanitizer
- Only dependencies:
 - fips202.c
 - sha2.c
 - aes.c
 - randombytes.c

The definition of "clean" ctd.

- API functions return 0 on success, negative on failure (WIP!)
 - 0 on success
 - Negative on failure (currently: partially)
- No dynamic memory allocations
- No branching on secret data (dynamically checked using valgrind)
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 - 0 on success
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- No branching on secret data (dynamically checked using valgrind)
- No access to secret memory locations (dynamically checked using valgrind)
- Separate subdirectories (without symlinks) for each parameter set of each scheme
- Builds under Linux, MacOS, and Windows
- All exported symbols are namespaced with PQCLEAN_SCHEMENAME_
- Each implementation comes with license and meta information in META.yml

Manually checked

- #ifdefs only for header encapsulation
- No stringification macros
- Output-parameter pointers in functions are on the left
- const arguments are labeled as const
- All exported symbols are namespaced inplace
- All integer types are of fixed size, using stdint.h types (including uint8_t instead of unsigned char)
- Integers used for indexing are of type size_t
- Variable declarations at the beginning (except in for (size_t i=...))

- pqm4 library and benchmarking suite: https://github.com/mupq/pqm4
- Code of Z_{2^m}[x] multiplication paper, including scripts: https://github.com/mupq/polymul-z2mx-m4
- Z_{2^m}[x] multiplication paper: https://cryptojedi.org/papers/#latticem4
- PQClean repository: https://github.com/PQClean/PQClean